

An ab Initio Based Global Potential Energy Surface Describing  $\text{CH}_5^+ \rightarrow \text{CH}_3^+ + \text{H}_2^\dagger$ 

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A full-dimensional, ab initio based potential energy surface (PES) for  $\text{CH}_5^+$ , which can describe dissociation is reported. The PES is a precise fit to 36173 coupled-cluster [CCSD(T)] calculations of electronic energies done using an aug-cc-pVTZ basis. The fit uses a polynomial basis that is invariant with respect to permutation of the five H atoms, and thus describes all 120 equivalent minima. The rms fitting error is  $78.1 \text{ cm}^{-1}$  for the entire data set of energies up to  $30\,000 \text{ cm}^{-1}$  and a normal-mode analysis of  $\text{CH}_5^+$  also verifies the accuracy of the fit. Two saddle points have been located on the surface as well and compared with previous theoretical work. The PES dissociates correctly to the fragments  $\text{CH}_3^+ + \text{H}_2$  and the equilibrium geometry and normal-mode analyses of these fragments are also presented. Diffusion Monte Carlo calculations are done for the zero-point energies of  $\text{CH}_5^+$  (and some isotopologs) as well as for the separated fragments of  $\text{CH}_5^+$ ,  $\text{CH}_3^+ + \text{H}_2$  and those of  $\text{CH}_4\text{D}^+$ ,  $\text{CH}_3^+ + \text{HD}$  and  $\text{CH}_2\text{D}^+ + \text{H}_2$ . Values of  $D_0$  are reported for these dissociations. A molecular dynamics calculation of  $\text{CH}_4\text{D}^+$  dissociation at one total energy is also performed to both validate the applicability of the PES for dynamics studies as well as to test a simple classical statistical prediction of the branching ratio of the dissociation products.

## I. Introduction

The cation  $\text{CH}_5^+$  plays an important role in astrochemistry<sup>1–3</sup> and possibly in combustion chemistry. This cation is also of great basic interest because it is known to be highly fluxional. There have been numerous theoretical studies<sup>4–16</sup> of  $\text{CH}_5^+$  since its discovery in mass spectrometry experiments in 1950s.<sup>17</sup> The first detailed insights into  $\text{CH}_5^+$  obtained from these calculations were that the minimum, denoted  $C_s(\text{I})$ , is a  $C_s$  structure that is characterized as a “ $\text{CH}_3$  tripod” with an “ $\text{H}_2$ ” attached to the carbon. This unusual structure was attributed to three-center two-electron bonding. In addition two saddle points, denoted  $C_s(\text{II})$  and  $C_{2v}$ , have been characterized. The most accurate calculations<sup>11</sup> report electronic energies of the  $C_s(\text{II})$  and  $C_{2v}$  saddle points of  $33.9$  and  $286.1 \text{ cm}^{-1}$  relative to the global minimum.

The nature of  $\text{CH}_5^+$  causes it to be quite resistant to direct experimental characterization. Results from mass spectrometric experiments by Hiraoka and co-workers<sup>18,19</sup> on  $\text{CH}_5^+$  are compatible with the 3-center, 2-electron bonded structure of  $C_s(\text{I})$  symmetry. However, this experiment is achieved by attaching methane molecules as the thermochemical sensors to the  $\text{CH}_5^+$  core.  $\text{CH}_5^+$  has complicated IR absorption spectrum. Oka and co-workers recorded the high-resolution infrared spectrum of  $\text{CH}_5^+$  in the range of  $2750\text{--}3150 \text{ cm}^{-1}$ . There are approximately 900 spectral lines<sup>20</sup> with considerable spectral congestion and to date these lines have not been assigned. Very recently Asvany et al. reported a low-resolution IR spectrum of  $\text{CH}_5^+$  (at  $110 \text{ K}$ ) in the range  $0\text{--}3500 \text{ cm}^{-1}$ .<sup>21</sup> Three broad bands were observed at  $1200$ ,  $2500$ , and  $3000 \text{ cm}^{-1}$ , with nearly continuous absorption in the range  $2500\text{--}3000 \text{ cm}^{-1}$ . The features were captured in a recent classical power spectrum reported by us using a full-dimensional potential energy surface

based on MP2/cc-pVTZ calculations.<sup>14</sup> A very similar finding though directly of the IR spectrum via the dipole correlation function using DFT-based direct dynamics was also reported along with this new spectrum.<sup>21</sup>

Theoretically, in addition to the electronic structure calculations, several dynamics studies have been reported. The first dynamical study showing the fluxional nature of  $\text{CH}_5^+$  was reported by Marx and Parrinello based on Car–Parrinello dynamics calculations and path-integral simulations.<sup>6,8,9</sup> More recently, we reported the zero point properties of  $\text{CH}_5^+$  and isotopologs obtained with classical molecular dynamics and quantum Diffusion Monte Carlo calculations by McCoy<sup>13</sup> and power spectra<sup>14</sup> of  $\text{CH}_5^+$  using our semi-global potential energy surface. This PES is a fit to ab initio MP2/cc-pVTZ energies, which is made explicitly invariant with respect to any permutation of the five H atoms. It does describe excitation of  $\text{CH}_5^+$  up to fairly high energies; however, it does not describe dissociation. Very recently other semiglobal PES and DMC calculations of the zero-point state were reported, based on CCSD(T)/aug-cc-pVTZ calculations.<sup>15</sup>

For a study of the important interstellar reaction<sup>3</sup>

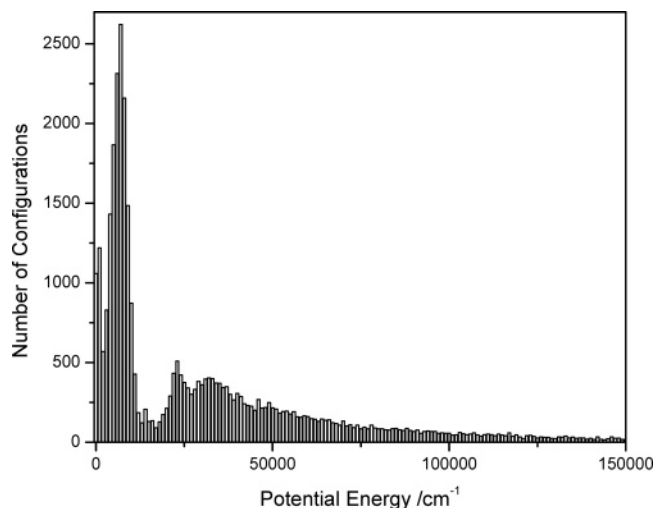


the PES of  $\text{CH}_5^+$  must extend to the dissociation limit  $\text{CH}_3^+ + \text{H}_2$ . The geometries used in the previous potentials<sup>12–14</sup> were focused in the configuration space around the global minimum of  $\text{CH}_5^+$  and so did not describe its dissociation. Motivated by this, we have developed a new potential energy surface that describes dissociation to fragments  $\text{CH}_3^+$  and  $\text{H}_2$  and present that surface and some calculations with it here.

The surface we describe here is constructed from 36173 CCSD(T) energies obtained with the aug-cc-pVTZ basis set using MOLPRO 2002.6.<sup>22</sup> Section II discusses the details of

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**Figure 1.** Energy distribution of geometries used in the fit.

the ab initio calculations, the fitting methods as well as tests of the accuracy of the PES in representing the ab initio data and a brief review of the Diffusion Monte Carlo calculations of the zero-point energy. In section III properties of the PES, the characteristic stationary point geometries, dissociation features, and monomer properties beyond dissociation limit are presented. Diffusion Monte Carlo calculations are also presented as is a short molecular dynamics calculation of the branching ratio of  $\text{CH}_4\text{D}^+$  to the two sets of products,  $\text{CH}_3^+ + \text{HD}$  and  $\text{CH}_2\text{D}^+ + \text{H}_2$ . Finally, a summary and conclusions are given in section IV.

## II. Methods and Calculation Details

**A. Ab Initio Calculations.** The previous PES we published<sup>12,13</sup> was obtained by fitting to MP2/cc-pVTZ ab initio data. The current fit uses a higher level of theory and larger basis set, CCSD(T)/aug-cc-pVTZ, for higher quality and a more accurate PES. For extending the PES to dissociation, many more ab initio points were obtained and they were created in several ways. First, geometries were directly taken from our previous calculations of the MP2-based PES. These were obtained using a combination of ab initio classical molecular dynamics (“direct-dynamics”), done at a lower level of ab initio theory and grids in normal coordinates.<sup>12–14</sup> Here we continued with this direct-dynamics approach but extended to higher total energies and supplemented those configurations with ones designed to focus on dissociation. Several direct-dynamics trajectories were done on very low theory/basis level which is MP2/cc-pVDZ but at higher given initial kinetic energy levels such as 10 500, 11 000, 11 500, and 12 000  $\text{cm}^{-1}$  for obtaining part of additional geometries. Second, a dissociation coordinate, denoted  $R$ , which is the distance between the  $\text{H}_2$  center of mass and the C atom of the  $\text{CH}_3^+$ , was used to obtain many additional configurations. Along this coordinate, which extended to 14.0 bohr, the potential was relaxed with respect to the remaining internal coordinates and the resulting path is our defined “dissociation minimum energy path”.

The energy distribution of the ab initio data used in the fit (relative to the global minimum energy) is shown in Figure 1. As seen, most of the data set is at energies below 50 000  $\text{cm}^{-1}$ , with a large concentration of energies below the dissociation energy of roughly 16 000  $\text{cm}^{-1}$ . Energies much above that value come from repulsive configurations where bonds are compressed.

Finally, fits (described below) were done and redone based on using those additional configurations obtained from doing MD and quantum DMC calculations on preliminary fits.

**B. Fitting the Potential Energy Surface.** The earlier fitting procedures for  $\text{CH}_5^+$ ,<sup>12,14</sup> and an early version of the  $\text{H}_3\text{O}_2^-$  PES<sup>23</sup> are closely related to the one we describe in this paper.  $\text{CH}_5^+$  has 12 vibrational degrees of freedom, however, to facilitate a description of the PES that is invariant with respect to a permutation of the five H atoms we use all 15 internuclear distances, as done previously.<sup>12,14,23</sup> The function describing the PES has the form<sup>12</sup>

$$V = p(x) + \sum_{i < j} q_{ij}(x)y_{ij} \quad (2)$$

where  $x$  is a 15-dimensional vector with components  $x_{ij} = \exp(-r_{ij})$ ,  $r_{ij}$  is the distance between nuclei  $i$  and  $j$ , and  $y_{ij}$  is given by

$$y_{ij} = \frac{e^{-r_{ij}}}{r_{ij}} \quad (3)$$

Here two functions  $p$  and  $q$  are used and they are seventh order and third-order multinomials of all  $x_{ij}$ , respectively. In addition,  $p$  and  $q$  are constructed to satisfy the permutation symmetry with respect to the five hydrogen atoms.<sup>12</sup> Here we also introduce a “reaction coordinate”  $R$ , which is the distance between the carbon atom and the center of mass of the  $\text{H}_2$  moiety. In the dissociation of  $\text{CH}_5^+$  the complex dissociates to two fragments  $\text{CH}_3^+$  and  $\text{H}_2$ . And  $R$  is large. Ab initio calculation of the super molecule,  $\text{CH}_3^+ + \text{H}_2$ , with the  $R$  large indicates that the potential of optimized  $\text{CH}_5^+$  geometry will approach the dissociation energy  $D_e$  as  $R$  goes to infinity. In the current fit,  $x_{ij} = \exp(-r_{ij})$  is used instead of  $x_{ij} = \ln(r_{ij})$ , which was used previously,<sup>14</sup> because the former can better describe the behavior of the potential in the dissociation region.

Some of the CCSD(T) energies were obtained at small C–H or H–H bond lengths where the potential is highly repulsive, cf. Figure 1. Thus, the fit used a weighted least squares approach such that geometries with energies above 30 000  $\text{cm}^{-1}$  have a weight of 0.2 while those below 30 000  $\text{cm}^{-1}$  have a weight of 1. The coefficients of the fit were computed using singular value decomposition.<sup>24</sup>

Finally, we extended the fit to properly describe the long-range electrostatic interaction, using a simple switching function<sup>25</sup> and an equation<sup>26</sup> describing the long range electrostatic interaction as described next.

**C. Long-Range Interaction.** As mentioned previously, the importance of reaction of  $\text{CH}_3^+ + \text{H}_2$  motivated us to extend our PES to its dissociation region; in other words,  $\text{CH}_5^+$  should be able to dissociate correctly to  $\text{CH}_3^+ + \text{H}_2$  on our PES. We plan to use the PES for dynamics calculations of the reaction 1 at very low relative translational energies of relevance to astrochemistry. Thus, we are also concerned about having the correct long-range behavior of the interaction. Rather than extend the ab initio calculations and fit to very long range, we decided to smoothly join the current fit to the known long-range behavior of the interaction. This was done using the following expression:

$$V = V_{\text{fit}}[1 - S(R)] + S(R)V_{\text{LR}}; \quad 11 \leq R \leq 15$$

$$V_{\text{LR}} \equiv V_{\text{ion-induced dipole}} + V_{\text{CH}_3^+} + V_{\text{H}_2} + D_e \quad (4)$$

where  $V_{\text{fit}}(R)$  is the potential energy obtained from the fit,

$V_{\text{ion-induced dipole}}$  is the analytically known long-range interaction,  $V_{\text{CH}_3^+}$  and  $V_{\text{H}_2}$  are the potentials of these two monomers.  $D_e$  is the dissociation energy and  $S(R)$  is a polynomial switching function that varies smoothly between 0 and 1 in a finite range.<sup>25</sup>  $S$  is given by

$$S(x) = \frac{a}{2}x^2 + \left(10 + \frac{b}{2} - \frac{3a}{2}\right)x^3 + \left(\frac{3a}{2} - b - 15\right)x^4 + \left(6 + \frac{b}{2} - \frac{a}{2}\right)x^5, \quad 0 \leq x \leq 1 \quad (5)$$

where  $a = f''(0)$  and  $b = f''(1)$ , and in the present case  $a = b = 0$  and  $x = (R - R_{\text{min}})/(R_{\text{max}} - R_{\text{min}})$ .  $V_{\text{CH}_3^+}$  and  $V_{\text{H}_2}$  were obtained from the  $\text{CH}_5^+$  fit itself but at a large separation where the interaction is quite small (see below for more details). In eq 4, the long-range term  $V_{\text{ion-induced dipole}}$  is given by the sum of charge-induced dipole ( $\text{H}_2$ ),  $U_4$  term<sup>26</sup>

$$U_4 = -\left[\frac{1}{2}\alpha + \frac{1}{3}(\alpha_{\parallel} - \alpha_{\perp})P_2(\cos \theta)\right]/R^4 \quad (6)$$

and the charge- $(\text{H}_2)$  quadrupole,  $U_3$  term<sup>26</sup>

$$U_3 = Q_{\text{H}_2}P_2(\cos \theta)/R^3 \quad (7)$$

$$P_2(\cos \theta) = \frac{1}{2}(3 \cos^2 \theta - 1) \quad (8)$$

where  $\theta$  is the angle between the vector  $\mathbf{R}$  and the  $\text{H}_2$  bond.  $\alpha, \alpha_{\parallel}$  and  $\alpha_{\perp}$  are the polarizabilities of the  $\text{H}_2$  molecule, and  $Q_{\text{H}_2}$  is its quadrupole moment.  $\alpha$  is the mean polarizability and given by<sup>27</sup>

$$\alpha = \frac{1}{3}(2\alpha_{\perp} + \alpha_{\parallel}) \quad (9)$$

$\alpha_{\parallel}$ ,  $\alpha_{\perp}$ , and  $Q_{\text{H}_2}$  were obtained using the cubic spline<sup>28</sup> interpolation based on the published polarizability data<sup>29</sup> and quadrupole moment data<sup>30</sup>

Finally, we have

$$V_{\text{ion-induced dipole}} = U_3 + U_4 \quad (10)$$

After some "experimentation", the switching range was chosen as  $11 \leq R \leq 15$  bohr. Note that in this switching range the fragments are quite far apart and very weakly interacting. Further the fragments are semirigid molecules and thus it is not necessary for the long-range potential to be permutationally invariant.

**D. Diffusion Monte Carlo calculations (DMC).** The DMC method is a statistical way to solve the time-dependent Schrödinger equation in imaginary time. In the current calculation, we use the version originally developed by Anderson<sup>31,32</sup> and implemented by our collaborator McCoy.<sup>33</sup> The DMC calculations in this paper follow the approach described in detail elsewhere<sup>12,13</sup> for the MP2-based PES. Specifically in the notation of those papers  $\alpha = 0.01$  hartree, the total propagation time = 10 000 time steps, with the time step = 10 au. Using these parameters we determined the zero-point energies (ZPEs) of  $\text{CH}_5^+$  and selected isotopologs as well as the combined ZPEs of  $\text{CH}_3^+ + \text{H}_2$  and selected isotopologs.

### III. Results and Discussion

**A. Properties of the PES. Fitting Accuracy.** The RMS fitting error vs  $E_{\text{max}}$  plot is presented in Figure 2 to show the accuracy of the PES. The error is  $78.1 \text{ cm}^{-1}$  for energies up to

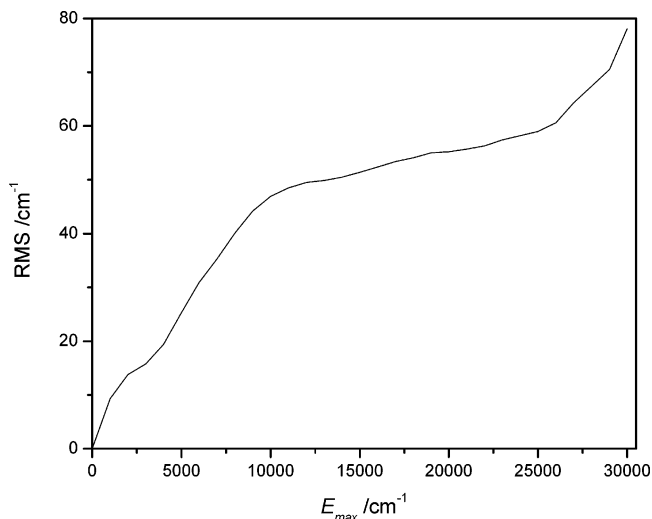


Figure 2. Fitting RMS error vs  $E_{\text{max}}$ .

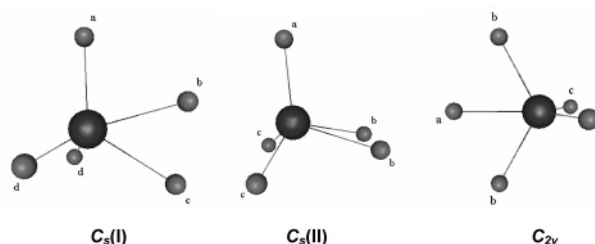


Figure 3. Representation of the three lowest energy stationary configurations of  $\text{CH}_5^+$  from the PES.  $C_s(\text{I})$  is the global minimum,  $C_s(\text{II})$  is the lower energy saddle point, and  $C_{2v}$  is the higher energy saddle point. Atom labels are given to aid in locating the movement of atoms among these stationary points.

$30\,000 \text{ cm}^{-1}$ , which is roughly twice as the dissociation energy. Therefore, we are very confident that the fit will be accurate enough for both quantum and classical (or semiclassical) vibrational and scattering calculations.

**Stationary Point Analysis.** The three stationary points of  $\text{CH}_5^+$  are the minimum and two saddle points, denoted  $C_s(\text{I})$ ,  $C_s(\text{II})$ , and  $C_{2v}$ , respectively. These were located on the PES using Newton's method. Considering the minimum as the reference energy, the energies of the  $C_s(\text{II})$  and  $C_{2v}$  saddle points on the PES are  $29.1$  and  $340.7 \text{ cm}^{-1}$ , respectively; the corresponding ab initio values are  $37.7$  and  $331.2 \text{ cm}^{-1}$  at the geometries of the PES saddle points. The molecular geometries of these three stationary points are shown in Figure 3, using the notation of Schreiner et al.<sup>5</sup> The internuclear distances of these structures are given in Table 1 along with previous benchmark results of Schreiner et al.<sup>5</sup> As seen there is excellent agreement between the present PES and these benchmark calculations.

Next consider the normal-mode frequencies associated with these stationary points. These are given in Table 1. Because of the high computational cost, we carried out a direct ab initio normal-mode analysis at the minimum only. As seen there is very good agreement between the PES frequencies and the ab initio ones. The current frequencies are also close to those reported previously for the MP2-based PES.<sup>14</sup>

**Fragment Properties.** The current PES dissociates correctly to the fragments  $\text{CH}_3^+$  and  $\text{H}_2$ . The minimum structure of  $\text{CH}_3^+$  is planar as it should be with C–H bond lengths equal to  $1.093 \text{ \AA}$  and the  $\text{H}_2$  equilibrium bond length is  $0.744 \text{ \AA}$ . These values compare very well with CCSD(T)/aug-cc-pVTZ ab initio calculations we did which give  $1.091$  and  $0.743 \text{ \AA}$ , respectively.

**TABLE 1: Geometry and Normal Mode Frequencies from the  $\text{CH}_5^+$  Potential Energy Surface at the Minimum and Two Saddle Points, Denoted  $C_s(\text{I})$ ,  $C_s(\text{II})$ , and  $C_{2v}$ , Respectively, with Comparisons with *ab Initio* Calculations Given**

	$C_s(\text{I})$ (Å)	$C_s(\text{II})$ (Å)	$C_{2v}$ (Å)
C–H <sub>a</sub>	1.108 (1.106) <sup>a</sup>	1.084 (1.084) <sup>a</sup>	1.163 (1.162) <sup>a</sup>
C–H <sub>b</sub>	1.197 (1.198)	1.200 (1.199)	1.087 (1.087)
C–H <sub>c</sub>	1.197 (1.197)	1.100 (1.098)	1.142 (1.140)
C–H <sub>d</sub>	1.088 (1.088)		
H <sub>2</sub>	0.952 (0.945)	0.945 (0.940)	

mode	$C_s(\text{I})$ (cm <sup>-1</sup> )	$C_s(\text{II})$ (cm <sup>-1</sup> )	$C_{2v}$ (cm <sup>-1</sup> )
1	199.9 (227.4) <sup>b</sup>	188.6i	698.5i
2	839.4 (831.3)	995.7	497.7
3	1296.7 (1284.3)	1151.2	1261.1
4	1303.5 (1291.2)	1340.3	1332.6
5	1477.7 (1464.1)	1482.1	1393.2
6	1499.9 (1492.9)	1507.1	1452.1
7	1586.7 (1595.8)	1603.2	1476.3
8	2417.9 (2430.1)	2401.1	2639.9
9	2707.7 (2714.9)	2728.8	2685.0
10	3001.0 (3011.0)	3037.8	2848.0
11	3132.9 (3130.2)	3090.5	3122.0
12	3224.4 (3224.4)	3236.1	3239.1

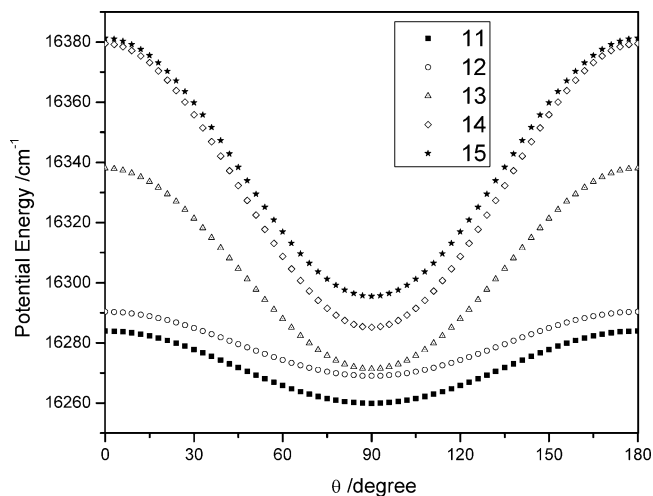
<sup>a</sup> Values in parentheses are CCSD(T)/TZ2P+*f* calculations of ref 5.<sup>b</sup> Values in parentheses are from present CCSD(T)/aug-cc-pVTZ *ab initio* calculations.**TABLE 2: Normal Mode Frequencies of  $\text{CH}_3^+$  and  $\text{H}_2$  from the  $\text{CH}_5^+$  PES**

mode	$\text{CH}_3^+$	$\text{H}_2$
1	1390.2 (1421.6) <sup>a</sup>	4377.0 (4400.2)
2	1412.1 (1429.0)	
3	1412.1 (1429.0)	
4	3031.2 (3039.3)	
5	3195.7 (3236.9)	
6	3195.7 (3236.9)	

<sup>a</sup> Numbers in parentheses are from present CCSD(T)/aug-cc-pVTZ calculations.

A normal-mode analysis was done on these fragments at a separation distance of  $R = 14$  bohr and the results are given in Table 2. The result for  $\text{H}_2$  is in excellent agreement with the benchmark value  $4401 \text{ cm}^{-1}$ . To compare the  $\text{CH}_3^+$  frequencies with *ab initio* we computed the optimized structure and normal-mode frequencies using CCSD(T)/aug-cc-pVTZ calculations. These are also given in Table 2. Very good agreement is seen with the results from the present PES.

**Behavior in the Switching Region.** As noted the present PES is not designed to describe the long-range electrostatic interaction and thus the switching approach described above was taken. The main purpose of this enhancement to the PES is to describe the long-range interaction for use in dynamics calculations. The long-range electrostatic interaction (cf. eqs 4–10) depends on the orientation of  $\text{H}_2$ ,  $\theta$ ,  $R$ , and also  $r_{\text{HH}}$ . The angular dependence of the combined potential in the switching region is shown in Figure 4, where  $r_{\text{HH}} = r_e$  and  $\text{CH}_3^+$  is also at equilibrium. At  $R = 11$  bohr, the angular dependence is strictly from the PES, and at  $R = 15$  bohr, it is from the added long-range potential. Obviously these two cannot be identical since they come from different sources; however, as seen the switch between the two is smooth even though there is larger angular dependence for the added potential than from the PES. The range of the angular variation is  $20 \text{ cm}^{-1}$  at 11 bohr, i.e., before the switching, and  $80 \text{ cm}^{-1}$  at 15 bohr, i.e., after the switching. These are small energies relative to the dissociation energy and they reflect the small differences in the

**Figure 4.** Angular dependence of potential energy on current PES within the switching region. The value in the legend is  $R$ , and the values are in bohrs and the angle  $\theta$  is defined in the text.**TABLE 3: Zero Point Energies of  $\text{CH}_5^+$  and Isotopologs**

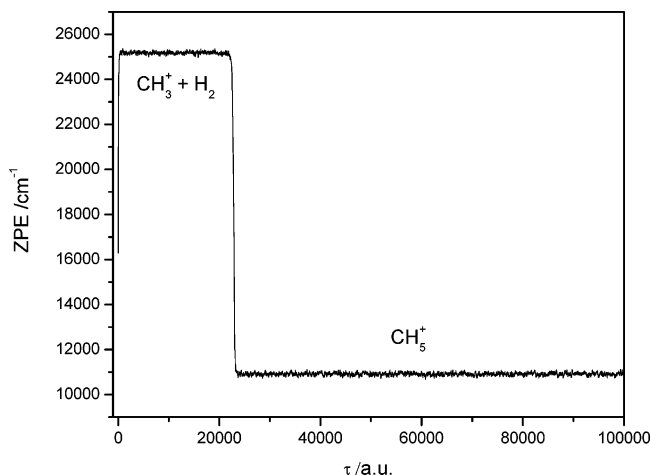
molecule	ZPE (cm <sup>-1</sup> ) <sup>a</sup>
$\text{CH}_5^+$	10917 (3)
$\text{CH}_4^+\text{D}$	10300 (6)
$\text{CH}_3^+\text{D}_2$	9694 (3)
$\text{CH}_2^+\text{D}_3$	9097 (6)
$\text{CH}^+\text{D}_4$	8563 (3)
$\text{CD}_5^+$	8044 (2)

<sup>a</sup> Statistical uncertainty is in parentheses.

long-range add-on to the PES and the PES itself. The dissociation energy  $D_e$ , obtained from the combined potential given by eq 4 obtained at  $R = 100$  bohr is  $16323 \text{ cm}^{-1}$ . This compares very well with the value obtained from direct *ab initio* calculations at 100 bohr of  $16321 \text{ cm}^{-1}$ .

**B. Diffusion Monte Carlo (DMC) Zero-Point Energies (ZPE) and  $D_0$ .** To obtain  $D_0$  for this floppy cation we calculated the ZPE of  $\text{CH}_5^+$  and the separated fragments and combined those numbers with  $D_e$  in the usual way. Accurate ZPEs were obtained using DMC calculations described above and are given in Table 3. The results compare well, i.e., differ by  $61 \text{ cm}^{-1}$  or less, with those reported on the previous MP2-based PES<sup>12,13</sup> (which does not dissociate) for  $\text{CH}_5^+$ ,  $\text{CH}_2\text{D}_3^+$ , and  $\text{CD}_5^+$ . Somewhat surprisingly the present ZPE for  $\text{CH}_5^+$  is  $177 \text{ cm}^{-1}$  lower than ZPE reported by Thompson et al.<sup>15</sup> who reported a DMC calculation of the ZPE using an interpolated PES based on the same *ab initio* method and basis (CCSD(T)/aug-cc-pVTZ) used in the present work.

Since the present PES can correctly describe the dissociation we also performed DMC calculations of the ZPE of the fragments  $\text{CH}_3^+ + \text{H}_2$  and the two sets of fragments of the  $\text{CH}_4\text{D}^+$  dissociation,  $\text{CH}_3^+ + \text{HD}$  and  $\text{CH}_2\text{D}^+ + \text{H}_2$ . These were done by separating the fragments and propagating using the full PES, as was done recently for the dissociation products of  $\text{H}_5^+$ ,  $\text{H}_3^+ + \text{H}_2$ .<sup>34</sup> The energy is shown in Figure 5 vs the (imaginary) propagation time for  $\text{CH}_3^+ + \text{H}_2$ . As seen there is a plateau region corresponding to the ZPE of the combined but noninteracting fragments (relative to the potential minimum at  $\text{CH}_5^+$ ), followed by a decline to another plateau corresponding to the ZPE of  $\text{CH}_5^+$ . From the ZPE calculations of the separated fragments and those of  $\text{CH}_5^+$  and  $\text{CH}_4\text{D}^+$  we obtain the following values of  $D_0$ :  $14316 \text{ cm}^{-1}$  for  $\text{CH}_5^+$ ,  $14650 \text{ cm}^{-1}$  for  $\text{CH}_4\text{D}^+$  to fragment to  $\text{CH}_3^+ + \text{HD}$ , and  $14367 \text{ cm}^{-1}$  to fragment to  $\text{CH}_2\text{D}^+ + \text{H}_2$ . Thus, the exoergicity of reaction 1



**Figure 5.** Energy vs (imaginary) time in DMC calculation of dissociated  $\text{CH}_5^+$  fragment  $\text{CH}_3^+ + \text{H}_2$ .

is predicted to be  $283 \text{ cm}^{-1}$  which is (fortuitously) in nearly perfect agreement with a calculated estimate (including an empirical scaling factor) of  $284 \text{ cm}^{-1}$ <sup>35</sup> and the measured value of  $260 \text{ cm}^{-1}$ .<sup>36</sup> We estimate a conservative statistical uncertainty of  $\pm 40 \text{ cm}^{-1}$  in these values. The absolute uncertainty in the  $D_0$ s is certainly larger than the statistical uncertainty but is probably less than  $100 \text{ cm}^{-1}$ .

**C. Molecular Dynamics Calculations of  $\text{CH}_4\text{D}^+$  Dissociation.** Finally we report a preliminary classical molecular dynamics simulation of the unimolecular  $\text{CH}_4\text{D}^+$  dissociation to form the two possible products  $\text{HD} + \text{CH}_3^+$  and  $\text{H}_2 + \text{CH}_2\text{D}^+$ . Of course any of the four H atoms can be found in the HD product, and the current potential does describe this multiplicity of products. The calculations were initiated at the global minimum with zero angular momentum and total energy of  $25\,000 \text{ cm}^{-1}$ , which is roughly  $D_e$  plus the zero-point energies of the fragments. This energy was randomly distributed as kinetic energy among the internal modes and 1000 trajectories were done for each single site substitution of the five H atoms for a total of 5000 trajectories. Dissociation was reached when the separation between fragments,  $R$ , reached 10 bohr. The branching ratio from these trajectories is 0.65 for  $\text{H}_2 + \text{CH}_2\text{D}^+$  and 0.35 for  $\text{HD} + \text{CH}_3^+$  in very good agreement with the classical statistical prediction of 0.6 and 0.4. A more sophisticated approach with a better assessment of the probability distribution of the possible D atom sites will be done in the future (here we assumed equal probability). Also, an attempt to enforce the zero-point energies of the fragments should be done in a future calculation.

#### IV. Summary and Conclusions

In this paper, we presented a full-dimensional potential energy surface (PES) for  $\text{CH}_5^+$  that dissociates to fragments  $\text{CH}_3^+ + \text{H}_2$ . We extended an approach used previously, which incorporates permutational symmetry into the fitting basis functions, by using a higher level of ab initio calculations, i.e., CCSD(T)/aug-cc-pVTZ and including more configurations to describe dissociation. Standard properties of the stationary configurations of the PES were shown to be in excellent agreement with previous benchmark calculations at these configurations. Properties of the  $\text{CH}_3^+$  and  $\text{H}_2$  fragments were also shown to be accurately obtained by the PES.

The analytical long-range ion-quadrupole and ion-induced dipole long-range behavior was added to the potential fit by means of a finite range switching function.

The PES was used in Diffusion Monte Carlo calculations of the zero-point energies of  $\text{CH}_5^+$ , deuterated isotopologs, and fragments. These together with the dissociation energy were used to predict  $D_0$  for  $\text{CH}_5^+$  and  $\text{CH}_4\text{D}^+$ . Finally a very brief molecular dynamics calculation of the product branching ratio of dissociation of  $\text{CH}_4\text{D}^+$  at one energy and zero total angular momentum showed very good agreement with a simple classical statistical prediction.

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